

Spearman's *[41 marks]*

The Malvern Aquatic Center hosted a 3 metre spring board diving event. The judges, Stan and Minsun awarded 8 competitors a score out of 10. The raw data is collated in the following table.

Competitors	A	B	C	D	E	F	G	H
Stan's score (x)	4.1	3	4.3	6	7.1	6	7.5	6
Minsun's score (y)	4.7	4.6	4.8	7.2	7.8	9	9.5	7.2

1a. Write down the value of the Pearson's product-moment correlation coefficient, r . *[2 marks]*

1b. Using the value of r , interpret the relationship between Stan's score and Minsun's score. *[2 marks]*

1c. Write down the equation of the regression line y on x . *[2 marks]*

1d. Use your regression equation from part (b) to estimate Minsun's score when Stan awards a perfect 10. *[2 marks]*

1e. State whether this estimate is reliable. Justify your answer. *[2 marks]*

The Commissioner for the event would like to find the Spearman's rank correlation coefficient.

1f. **Copy** and complete the information in the following table. *[2 marks]*

Competitors	A	B	C	D	E	F	G	H
Stan's Rank		8					1	4
Minsun's Rank		8					1	4.5

1g. Find the value of the Spearman's rank correlation coefficient, r_s . *[2 marks]*

1h. Comment on the result obtained for r_s . *[2 marks]*

- 1i. The Commissioner believes Minsun's score for competitor G is too high [1 mark] and so decreases the score from 9.5 to 9.1.

Explain why the value of the Spearman's rank correlation coefficient r_s does not change.

Kayla wants to measure the extent to which two judges in a gymnastics competition are in agreement. Each judge has ranked the seven competitors, as shown in the table, where 1 is the highest ranking and 7 is the lowest.

Competitor	A	B	C	D	E	F	G
Judge 1	1	2	3	3	5	6	6
Judge 2	2	3	1	4	5	5	7

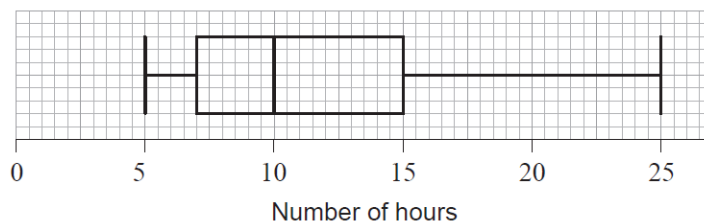
- 2a. Calculate Spearman's rank correlation coefficient for this data. [5 marks]

- 2b. State what conclusion Kayla can make from the answer in part (a). [1 mark]

As part of his mathematics exploration about classic books, Jason investigated the time taken by students in his school to read the book *The Old Man and the Sea*. He collected his data by stopping and asking students in the school corridor, until he reached his target of 10 students from **each** of the literature classes in his school.

- 3a. State which of the two sampling methods, systematic or quota, Jason has [1 mark] used.

Jason constructed the following box and whisker diagram to show the number of hours students in the sample took to read this book.



- 3b. Write down the median time to read the book. [1 mark]

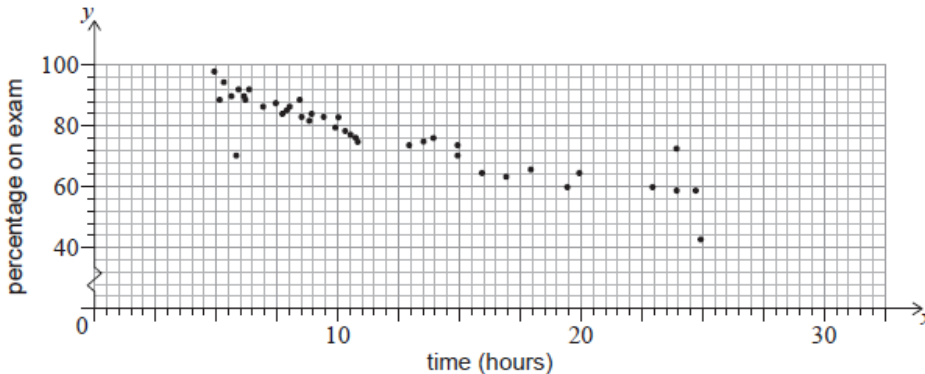
- 3c. Calculate the interquartile range. [2 marks]

Mackenzie, a member of the sample, took 25 hours to read the novel. Jason believes Mackenzie's time is not an outlier.

3d. Determine whether Jason is correct. Support your reasoning.

[4 marks]

For each student interviewed, Jason recorded the time taken to read *The Old Man and the Sea* (x), measured in hours, and paired this with their percentage score on the final exam (y). These data are represented on the scatter diagram.



3e. Describe the correlation.

[1 mark]

Jason correctly calculates the equation of the regression line y on x for these students to be

$$y = -1.54x + 98.8.$$

He uses the equation to estimate the percentage score on the final exam for a student who read the book in 1.5 hours.

3f. Find the percentage score calculated by Jason.

[2 marks]

3g. State whether it is valid to use the regression line y on x for Jason's estimate. Give a reason for your answer.

[2 marks]

Jason found a website that rated the 'top 50' classic books. He randomly chose eight of these classic books and recorded the number of pages. For example, Book H is rated 44th and has 281 pages. These data are shown in the table.

Book	A	B	C	D	E	F	G	H
Number of pages (n)	4215	863	585	1225	366	209	624	281
Top 50 rating (r)	1	2	5	7	13	22	40	44

Jason intends to analyse the data using Spearman's rank correlation coefficient, r_s .

3h. Copy and complete the information in the following table.

[2 marks]

Book	A	B	C	D	E	F	G	H
Rank – Number of pages	1							
Rank – Top 50 Rating	1							

3i. Calculate the value of r_s .

[2 marks]

3j. Interpret your result.

[1 mark]