

# Course at a Glance

## Plan

The Course at a Glance provides a useful visual organization of the AP Calculus AB and AP Calculus BC curricular components, including:

- Sequence of units, along with approximate weighting and suggested pacing. Please note, pacing is based on 45-minute class periods, meeting five days each week for a full academic year.
- Progression of topics within each unit.
- Spiraling of the big ideas and mathematical practices across units.

## Teach

### MATHEMATICAL PRACTICES

Mathematical practices spiral throughout the course.

- |  |                                     |
|--|-------------------------------------|
| <b>1</b> Implementing Mathematical Processes | <b>3</b> Justification              |
| <b>2</b> Connecting Representations          | <b>4</b> Communication and Notation |

### BIG IDEAS

Big ideas spiral across topics and units.

- |                   |                                  |
|-------------------|----------------------------------|
| <b>CHA</b> Change | <b>FUN</b> Analysis of Functions |
| <b>LIM</b> Limits |                                  |

### BC ONLY

The purple shading represents BC only content.

## Assess

Assign the Personal Progress Checks—either as homework or in class—for each unit. Each Personal Progress Check contains formative multiple-choice and free-response questions. The feedback from the Personal Progress Checks shows students the areas where they need to focus.

1

**UNIT 1**

## Limits and Continuity

AP EXAM WEIGHTING

10–12% AB    4–7% BC

CLASS PERIODS

~22–23 AB    ~13–14 BC

2

**UNIT 2**

## Differentiation: Definition and Basic Derivative Rules

AP EXAM WEIGHTING

10–12% AB    4–7% BC

CLASS PERIODS

~13–14 AB    ~9–10 BC

|            |          |   |
|------------|----------|---|
| <b>CHA</b> | <b>2</b> | <b>1.1</b> Introducing Calculus: Can Change Occur at an Instant?    |
| <b>LIM</b> | <b>2</b> | <b>1.2</b> Defining Limits and Using Limit Notation                 |
| <b>LIM</b> | <b>2</b> | <b>1.3</b> Estimating Limit Values from Graphs                      |
| <b>LIM</b> | <b>2</b> | <b>1.4</b> Estimating Limit Values from Tables                      |
| <b>LIM</b> | <b>1</b> | <b>1.5</b> Determining Limits Using Algebraic Properties of Limits  |
| <b>LIM</b> | <b>1</b> | <b>1.6</b> Determining Limits Using Algebraic Manipulation          |
| <b>LIM</b> | <b>1</b> | <b>1.7</b> Selecting Procedures for Determining Limits              |
| <b>LIM</b> | <b>3</b> | <b>1.8</b> Determining Limits Using the Squeeze Theorem             |
| <b>LIM</b> | <b>2</b> | <b>1.9</b> Connecting Multiple Representations of Limits            |
| <b>LIM</b> | <b>3</b> | <b>1.10</b> Exploring Types of Discontinuities                      |
| <b>LIM</b> | <b>3</b> | <b>1.11</b> Defining Continuity at a Point                          |
| <b>LIM</b> | <b>1</b> | <b>1.12</b> Confirming Continuity over an Interval                  |
| <b>LIM</b> | <b>1</b> | <b>1.13</b> Removing Discontinuities                                |
| <b>LIM</b> | <b>3</b> | <b>1.14</b> Connecting Infinite Limits and Vertical Asymptotes      |
| <b>LIM</b> | <b>2</b> | <b>1.15</b> Connecting Limits at Infinity and Horizontal Asymptotes |
| <b>FUN</b> | <b>3</b> | <b>1.16</b> Working with the Intermediate Value Theorem (IVT)       |

|            |          |  |
|------------|----------|--|
| <b>CHA</b> | <b>2</b> | <b>2.1</b> Defining Average and Instantaneous Rates of Change at a Point                                 |
| <b>CHA</b> | <b>1</b> | <b>2.2</b> Defining the Derivative of a Function and Using Derivative Notation                           |
| <b>4</b>   | <b>4</b> |  |
| <b>CHA</b> | <b>1</b> | <b>2.3</b> Estimating Derivatives of a Function at a Point   |
| <b>FUN</b> | <b>3</b> | <b>2.4</b> Connecting Differentiability and Continuity: Determining When Derivatives Do and Do Not Exist |
| <b>FUN</b> | <b>1</b> | <b>2.5</b> Applying the Power Rule   |
| <b>FUN</b> | <b>1</b> | <b>2.6</b> Derivative Rules: Constant, Sum, Difference, and Constant Multiple                            |
| <b>FUN</b> | <b>1</b> | <b>2.7</b> Derivatives of $\cos x$ , $\sin x$ , $e^x$ , and $\ln x$                                      |
| <b>FUN</b> | <b>1</b> | <b>2.8</b> The Product Rule  |
| <b>FUN</b> | <b>1</b> | <b>2.9</b> The Quotient Rule   |
| <b>FUN</b> | <b>1</b> | <b>2.10</b> Finding the Derivatives of Tangent, Cotangent, Secant, and/or Cosecant Functions             |

### Personal Progress Check 1

Multiple-choice: ~45 questions  
Free-response: 3 questions (partial)

### Personal Progress Check 2

Multiple-choice: ~30 questions  
Free-response: 3 questions (partial)

**NOTE:** Partial versions of the free-response questions are provided to prepare students for more complex, full questions that they will encounter on the AP Exam.



### UNIT 3

## Differentiation: Composite, Implicit, and Inverse Functions

AP EXAM WEIGHTING **9–13% AB** **4–7% BC**

CLASS PERIODS **~10–11 AB** **~8–9 BC**

|          |   |
|----------|---|
| FUN<br>1 | <b>3.1 The Chain Rule</b>                                   |
| FUN<br>1 | <b>3.2 Implicit Differentiation</b>                         |
| FUN<br>3 | <b>3.3 Differentiating Inverse Functions</b>                |
| FUN<br>1 | <b>3.4 Differentiating Inverse Trigonometric Functions</b>  |
| FUN<br>1 | <b>3.5 Selecting Procedures for Calculating Derivatives</b> |
| FUN<br>1 | <b>3.6 Calculating Higher-Order Derivatives</b>             |

### Personal Progress Check 3

Multiple-choice: ~15 questions  
Free-response: 3 questions (partial/full)

### UNIT 4

## Contextual Applications of Differentiation

AP EXAM WEIGHTING **10–15% AB** **6–9% BC**

CLASS PERIODS **~10–11 AB** **~6–7 BC**

|          |   |
|----------|---|
| CHA<br>1 | <b>4.1 Interpreting the Meaning of the Derivative in Context</b>                      |
| CHA<br>1 | <b>4.2 Straight-Line Motion: Connecting Position, Velocity, and Acceleration</b>      |
| CHA<br>2 | <b>4.3 Rates of Change in Applied Contexts Other Than Motion</b>                      |
| CHA<br>1 | <b>4.4 Introduction to Related Rates</b>  |
| CHA<br>3 | <b>4.5 Solving Related Rates Problems</b>   |
| CHA<br>1 | <b>4.6 Approximating Values of a Function Using Local Linearity and Linearization</b> |
| LIM<br>3 | <b>4.7 Using L'Hospital's Rule for Determining Limits of Indeterminate Forms</b>      |

### Personal Progress Check 4

Multiple-choice: ~15 questions  
Free-response: 3 questions

### UNIT 5

## Analytical Applications of Differentiation

AP EXAM WEIGHTING **15–18% AB** **8–11% BC**

CLASS PERIODS **~15–16 AB** **~10–11 BC**

|               |  |
|---------------|--|
| FUN<br>3      | <b>5.1 Using the Mean Value Theorem</b>  |
| FUN<br>3      | <b>5.2 Extreme Value Theorem, Global Versus Local Extrema, and Critical Points</b> |
| FUN<br>2      | <b>5.3 Determining Intervals on Which a Function Is Increasing or Decreasing</b>   |
| FUN<br>3      | <b>5.4 Using the First Derivative Test to Determine Relative (Local) Extrema</b>   |
| FUN<br>1      | <b>5.5 Using the Candidates Test to Determine Absolute (Global) Extrema</b>        |
| FUN<br>2      | <b>5.6 Determining Concavity of Functions over Their Domains</b>                   |
| FUN<br>3      | <b>5.7 Using the Second Derivative Test to Determine Extrema</b>                   |
| FUN<br>2      | <b>5.8 Sketching Graphs of Functions and Their Derivatives</b>                     |
| FUN<br>2      | <b>5.9 Connecting a Function, Its First Derivative, and Its Second Derivative</b>  |
| FUN<br>2      | <b>5.10 Introduction to Optimization Problems</b>                                  |
| FUN<br>3      | <b>5.11 Solving Optimization Problems</b>  |
| FUN<br>1<br>3 | <b>5.12 Exploring Behaviors of Implicit Relations</b>                              |

### Personal Progress Check 5

Multiple-choice: ~35 questions  
Free-response: 3 questions



# UNIT 6

## Integration and Accumulation of Change

AP EXAM WEIGHTING **17–20% AB** **17–20% BC**

CLASS PERIODS **~18–20 AB** **~15–16 BC**

|          |  |
|----------|--|
| CHA<br>4 | 6.1 Exploring Accumulations of Change  |
| LIM<br>1 | 6.2 Approximating Areas with Riemann Sums                                      |
| LIM<br>2 | 6.3 Riemann Sums, Summation Notation, and Definite Integral Notation           |
| FUN<br>1 | 6.4 The Fundamental Theorem of Calculus and Accumulation Functions             |
| FUN<br>2 | 6.5 Interpreting the Behavior of Accumulation Functions Involving Area         |
| FUN<br>3 | 6.6 Applying Properties of Definite Integrals                                  |
| FUN<br>3 | 6.7 The Fundamental Theorem of Calculus and Definite Integrals                 |
| FUN<br>4 | 6.8 Finding Antiderivatives and Indefinite Integrals: Basic Rules and Notation |
| FUN<br>1 | 6.9 Integrating Using Substitution   |
| FUN<br>1 | 6.10 Integrating Functions Using Long Division and Completing the Square       |
| FUN<br>1 | 6.11 Integrating Using Integration by Parts<br>BC ONLY                         |
| FUN<br>1 | 6.12 Using Linear Partial Fractions<br>BC ONLY                                 |
| LIM<br>1 | 6.13 Evaluating Improper Integrals<br>BC ONLY                                  |
| FUN<br>1 | 6.14 Selecting Techniques for Antidifferentiation                              |

### Personal Progress Check 6

Multiple-choice:

- ~25 questions (AB)
- ~35 questions (BC)

Free-response: 3 questions

# UNIT 7

## Differential Equations

AP EXAM WEIGHTING **6–12% AB** **6–9% BC**

CLASS PERIODS **~8–9 AB** **~9–10 BC**

|          |   |
|----------|---|
| FUN<br>2 | 7.1 Modeling Situations with Differential Equations                                   |
| FUN<br>3 | 7.2 Verifying Solutions for Differential Equations                                    |
| FUN<br>2 | 7.3 Sketching Slope Fields  |
| FUN<br>4 | 7.4 Reasoning Using Slope Fields  |
| FUN<br>1 | 7.5 Approximating Solutions Using Euler's Method<br>BC ONLY                           |
| FUN<br>1 | 7.6 Finding General Solutions Using Separation of Variables                           |
| FUN<br>1 | 7.7 Finding Particular Solutions Using Initial Conditions and Separation of Variables |
| FUN<br>3 | 7.8 Exponential Models with Differential Equations                                    |
| FUN<br>3 | 7.9 Logistic Models with Differential Equations<br>BC ONLY                            |

### Personal Progress Check 7

Multiple-choice:

- ~15 questions (AB)
- ~20 questions (BC)

Free-response: 3 questions

# UNIT 8

## Applications of Integration

AP EXAM WEIGHTING **10–15% AB** **6–9% BC**

CLASS PERIODS **~19–20 AB** **~13–14 BC**

|          |  |
|----------|--|
| CHA<br>1 | 8.1 Finding the Average Value of a Function on an Interval                       |
| CHA<br>1 | 8.2 Connecting Position, Velocity, and Acceleration of Functions Using Integrals |
| CHA<br>3 | 8.3 Using Accumulation Functions and Definite Integrals in Applied Contexts      |
| CHA<br>4 | 8.4 Finding the Area Between Curves Expressed as Functions of $x$                |
| CHA<br>1 | 8.5 Finding the Area Between Curves Expressed as Functions of $y$                |
| CHA<br>2 | 8.6 Finding the Area Between Curves That Intersect at More Than Two Points       |
| CHA<br>3 | 8.7 Volumes with Cross Sections: Squares and Rectangles                          |
| CHA<br>3 | 8.8 Volumes with Cross Sections: Triangles and Semicircles                       |
| CHA<br>3 | 8.9 Volume with Disc Method: Revolving Around the $x$ - or $y$ -Axis             |
| CHA<br>2 | 8.10 Volume with Disc Method: Revolving Around Other Axes                        |
| CHA<br>4 | 8.11 Volume with Washer Method: Revolving Around the $x$ - or $y$ -Axis          |
| CHA<br>2 | 8.12 Volume with Washer Method: Revolving Around Other Axes                      |
| CHA<br>3 | 8.13 The Arc Length of a Smooth, Planar Curve and Distance Traveled<br>BC ONLY   |

### Personal Progress Check 8

Multiple-choice: ~30 questions

Free-response: 3 questions



# UNIT 9

## Parametric Equations, Polar Coordinates, and Vector-Valued Functions BC ONLY

AP EXAM WEIGHTING **N/A** AB **11–12%** BC

CLASS PERIODS **N/A** AB **~10–11** BC

|          |   |
|----------|---|
| CHA<br>2 | 9.1 Defining and Differentiating Parametric Equations                           |
| CHA<br>1 | 9.2 Second Derivatives of Parametric Equations                                  |
| CHA<br>1 | 9.3 Finding Arc Lengths of Curves Given by Parametric Equations                 |
| CHA<br>1 | 9.4 Defining and Differentiating Vector-Valued Functions                        |
| FUN<br>1 | 9.5 Integrating Vector-Valued Functions   |
| FUN<br>1 | 9.6 Solving Motion Problems Using Parametric and Vector-Valued Functions        |
| FUN<br>2 | 9.7 Defining Polar Coordinates and Differentiating in Polar Form                |
| CHA<br>3 | 9.8 Find the Area of a Polar Region or the Area Bounded by a Single Polar Curve |
| CHA<br>3 | 9.9 Finding the Area of the Region Bounded by Two Polar Curves                  |

### Personal Progress Check 9

Multiple-choice: ~25 questions  
Free-response: 3 questions

# UNIT 10

## Infinite Sequences and Series BC ONLY

AP EXAM WEIGHTING **N/A** AB **17–18%** BC

CLASS PERIODS **N/A** AB **~17–18** BC

|          |   |
|----------|---|
| LIM<br>3 | 10.1 Defining Convergent and Divergent Infinite Series      |
| LIM<br>3 | 10.2 Working with Geometric Series                          |
| LIM<br>3 | 10.3 The $n$ th Term Test for Divergence                    |
| LIM<br>3 | 10.4 Integral Test for Convergence                          |
| LIM<br>3 | 10.5 Harmonic Series and $p$ -Series                        |
| LIM<br>3 | 10.6 Comparison Tests for Convergence                       |
| LIM<br>3 | 10.7 Alternating Series Test for Convergence                |
| LIM<br>3 | 10.8 Ratio Test for Convergence                             |
| LIM<br>3 | 10.9 Determining Absolute or Conditional Convergence        |
| LIM<br>1 | 10.10 Alternating Series Error Bound                        |
| LIM<br>3 | 10.11 Finding Taylor Polynomial Approximations of Functions |
| LIM<br>2 | 10.12 Lagrange Error Bound                                  |
| LIM<br>1 | 10.13 Radius and Interval of Convergence of Power Series    |
| LIM<br>2 | 10.14 Finding Taylor or Maclaurin Series for a Function     |
| LIM<br>3 | 10.15 Representing Functions as Power Series                |

### Personal Progress Check 10

Multiple-choice: ~45 questions  
Free-response: 3 questions