## Quadrilaterals

## Quadrilateral

A quadrilateral is the union of four line-segments determined by four distinct coplanar points of which no three are collinear and the line-segments intersect only at end points.

For $A B C D$ to be quadrilateral, following condition are required
a) The four points $A, B, C$ and $D$ must be distinct and co-planar.
b) No three of points $A, B, C$ and $D$ are co-linear.
c) Line segments i.e. $A B, B C, C D, D A$ intersect at their end points only.


A quadrilateral is a four-sided polygon with four angles. There are many kinds of quadrilaterals. The five most common types are the parallelogram, the rectangle, the square, the trapezoid, and the rhombus.

## Angle Property of Quadrilateral

1) Sum of all the interior angles is $360^{\circ}$
2) Sum of all the exterior angles is $360^{\circ}$

## Parallelogram

A quadrilateral which has both pairs of opposite sides parallel is called a parallelogram. Its properties are:

- The opposite sides of a parallelogram are equal.
- The opposite angles of a parallelogram are equal.
- The diagonals of a parallelogram bisect each other.
- The diagonal of a parallelogram divide into two congruent triangles


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A quadrilateral is said to a parallelogram if
Opposite sides are equal OR Opposite angles are equal OR Diagonal bisects each other OR A pair of opposite are parallel and equal

## Trapezium

A quadrilateral which has one pair of opposite sides parallel is called a trapezium.


## Rhombus

Rhombus is a parallelogram in which any pair of adjacent sides is equal.
Properties of a rhombus:

- All sides of a rhombus are equal
- The opposite angles of a rhombus are equal
- The diagonals of a rhombus bisect each other at right angles.



## Rectangle

A parallelogram which has one of its angles a right angle is called a rectangle.
Properties of a rectangle are:

- The opposite sides of a rectangle are equal
- Each angle of a rectangle is a right-angle.
- The diagonals of a rectangle are equal.
- The diagonals of a rectangle bisect each other.

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## Square

A quadrilateral, all of whose sides are equal and all of whose angles are right angles.
Properties of square are:

- All the sides of a square are equal.
- Each of the angles measures $90^{\circ}$.
- The diagonals of a square bisect each other at right angles.
- The diagonals of a square are equal.


All the quadrilaterals can be shown in Venn diagram like this

## Venn Diagram



## Some important facts

a) A square is always a parallelogram.

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b) A square is always a rectangle.
c) A rhombus can be square.
e) A rectangle has four right angles.

## Mid-point Theorem for Triangles

## Theorem-I

The line segment joining the mid points of the two sides of the triangle is parallel to the third side


## Theorem-II

A line drawn through mid point of one side of a triangle and parallel to another side bisect the third side of the triangle

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