

**Calculus**  
**Paperweight Volumes**

Name \_\_\_\_\_

Find each of the following volumes for solids who are formed from regions with known cross sections.

1. Find the volume of solid S whose base is the region in the  $xy$ -plane bounded by the curves  $y = x^2$  and  $y = 8 - x^2$  and whose cross-sections perpendicular to the  $x$ -axis are squares with one side in the  $xy$ -plane.
2. Find the volume of solid S whose base is the region in the  $xy$ -plane bounded by the  $x$ -axis,  $y$ -axis and line  $y = -x + 5$  and whose cross-sections perpendicular to the  $y$ -axis are equilateral triangles with one side in the  $xy$ -plane.
3. Find the volume of solid S whose base is the region in the  $xy$ -plane bounded by the  $x$ -axis,  $y$ -axis and line  $y = -x + 5$  and whose cross-sections perpendicular to the  $x$ -axis are semicircles with diameters in the  $xy$ -plane.
4. Find the volume of solid S whose base is a circle of radius 2 and whose cross-sections perpendicular to the  $x$ -axis are isosceles right triangles with their hypotenuses in the  $xy$ -plane.
5. Find the volume of solid S who is built from an ellipse with a semi-major axis of 4 and a semi-minor axis of 2 in the  $xy$ -plane and whose cross-sections perpendicular to the  $y$ -axis are circles with their diameters in the  $xy$ -plane.