# Geometric [46 marks]

#### **1a.** [2 marks]

A ball is dropped from a height of 1.8 metres and bounces on the ground. The maximum height reached by the ball, after each bounce, is 85% of the previous maximum height.



Show that the maximum height reached by the ball after it has bounced for the sixth time is 68 cm, to the nearest cm.

#### **1b.** [2 marks]

Find the number of times, after the first bounce, that the maximum height reached is greater than 10 cm.

#### **1c.** [3 marks]

Find the total **vertical** distance travelled by the ball from the point at which it is dropped until the fourth bounce.

#### **2a.** [2 marks]

The admissions team at a new university are trying to predict the number of student applications they will receive each year.

Let n be the number of years that the university has been open. The admissions team collect the following data for the first two years.

Year, n	Number of applications received in year $n$
1	12300
2	12 669

Calculate the percentage increase in applications from the first year to the second year.

## **2b.** [1 mark]

It is assumed that the number of students that apply to the university each year will follow a geometric sequence,  $u_n$ .

Write down the common ratio of the sequence.

## **2c.** [1 mark]

Find an expression for  $u_n$ .

### 2d. [2 marks]

Find the number of student applications the university expects to receive when n = 11. Express your answer to the nearest integer.

## **3a.** [2 marks]

Mia baked a very large apple pie that she cuts into slices to share with her friends. The smallest slice is cut first. The volume of each successive slice of pie forms a geometric sequence.

The second smallest slice has a volume of  $30 \text{ cm}^3$ . The fifth smallest slice has a volume of  $240 \text{ cm}^3$ .

Find the common ratio of the sequence.

**3b.** [2 marks]

Find the volume of the smallest slice of pie.

**3c.** [2 marks]

The apple pie has a volume of  $61425 \text{ cm}^3$ .

Find the total number of slices Mia can cut from this pie.

**4a.** [2 marks]

A geometric sequence has a first term of  $\frac{8}{3}$  and a fourth term of 9.

Find the common ratio.

**4b.** [1 mark]

Write down the second term of this sequence.

**6.** [3 marks]

The first three terms of a geometric sequence are  $\ln x^{16}$ ,  $\ln x^8$ ,  $\ln x^4$ , for x > 0.

Find the common ratio.

**7.** [1 mark]

Consider the geometric sequence  $u_1 = 18$ ,  $u_2 = 9$ ,  $u_3 = 4.5$ , ....

Write down the common ratio of the sequence.