## Geometric [46 marks]

1a. [2 marks]
A ball is dropped from a height of 1.8 metres and bounces on the ground. The maximum height reached by the ball, after each bounce, is $85 \%$ of the previous maximum height.


Show that the maximum height reached by the ball after it has bounced for the sixth time is 68 cm , to the nearest cm.

1b. [2 marks]
Find the number of times, after the first bounce, that the maximum height reached is greater than 10 cm .

## 1c. [3 marks]

Find the total vertical distance travelled by the ball from the point at which it is dropped until the fourth bounce.

2a. [2 marks]
The admissions team at a new university are trying to predict the number of student applications they will receive each year.

Let $n$ be the number of years that the university has been open. The admissions team collect the following data for the first two years.

| Year, $\boldsymbol{n}$ | Number of applications received in year $\boldsymbol{n}$ |
| :---: | :---: |
| 1 | 12300 |
| 2 | 12669 |

Calculate the percentage increase in applications from the first year to the second year.
2b. [1 mark]
It is assumed that the number of students that apply to the university each year will follow a geometric sequence, $u_{n}$.

Write down the common ratio of the sequence.
2c. [1 mark]
Find an expression for $u_{n}$.
2d. [2 marks]
Find the number of student applications the university expects to receive when $n=11$. Express your answer to the nearest integer.

3a. [2 marks]
Mia baked a very large apple pie that she cuts into slices to share with her friends. The smallest slice is cut first. The volume of each successive slice of pie forms a geometric sequence.

The second smallest slice has a volume of $30 \mathrm{~cm}^{3}$. The fifth smallest slice has a volume of $240 \mathrm{~cm}^{3}$.

Find the common ratio of the sequence.
3b. [2 marks]
Find the volume of the smallest slice of pie.
3c. [2 marks]
The apple pie has a volume of $61425 \mathrm{~cm}^{3}$.
Find the total number of slices Mia can cut from this pie.
4a. [2 marks]
A geometric sequence has a first term of $\frac{8}{3}$ and a fourth term of 9 .
Find the common ratio.
4b. [1 mark]

Write down the second term of this sequence.
6. [3 marks]

The first three terms of a geometric sequence are $\ln x^{16}, \ln x^{8}, \ln x^{4}$, for $x>0$.
Find the common ratio.
7. [1 mark]

Consider the geometric sequence $u_{1}=18, u_{2}=9, u_{3}=4.5, \ldots$.
Write down the common ratio of the sequence.

